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## PRESSURE LOSS

- Pipe losses P2 and P3 take place inside the drill pipe and drill collars.
- Annular losses P4 and P5 take place around the drill collar and drill pipe.
- The magnitudes of P2, P3, P4 and P5 depend on:
- 1. Dimension of drill pipe (or drill collars), e.g. inside and outside diameter and length.
- 2. Mud rheological properties, which include mud weight, plastic viscosity, and yield point.
- 3. Type of flow, which can be laminar, or turbulent.



# EQUATIONS

• 
$$\Delta P_{bit} = P_{stand pipe} - (P_1 + P_2 + P_3 + P_4 + P_5)$$
  
•  $V_n \left(\frac{ft}{min}\right) = 33.36 \sqrt{\frac{\Delta P_{bit}}{\rho}}$   
•  $A_n(in^2) = \frac{0.32*Q}{V_n}$   
•  $d_n = 32 \sqrt{\frac{4*A_n}{3*\pi}}$   
• Q= gpm

• HHP = 
$$\frac{Q P_T}{1714 e_v e_m}$$

• **B.H.C.P.** = 
$$0.052\rho D + \Delta P_{ap} + \Delta P_{ac}$$

• E. C. D. = MW + 
$$\frac{\Delta P_{ap} + \Delta P_{ac}}{0.052 \times D}$$

- HHP: Hydraulic Horse Power
- BHCP: Bottom Hole Circulating Pressure
- ECD: Equivalent Circulating Density



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#### PRACTICAL HYDRAULICS EQUATIONS PROCEDURE

- 1. Calculate surface pressure losses.
- 2. Decide on which model to use: Bingham Plastic or Power Law.
- 3. Calculate pressure loss inside the drill pipe first then inside drill collars as follows:
- Calculate the critical velocity of flow  $V_c$ .
- Calculate actual average velocity of flow  $V_a$  or  $\acute{V}$ .
- $V_a > V_c$  Turbulent flow Use the appropriate equation to calculate pressure drop.
- $V_a < V_c$  Laminar flow Use the appropriate equation to calculate pressure drop.
- 4. Divide the annulus into open and cased sections.



5. Calculate annular flow around drill collars (or BHA) as follows:

- Calculate the critical velocity of flow  $V_c$ .
- Calculate actual average velocity of flow  $V_a$  or  $\acute{V}$ .
- $V_a > V_c$  Turbulent flow Use the appropriate equation to calculate pressure drop.
- $V_a < V_c$  Laminar flow Use the appropriate equation to calculate pressure drop.

6. Repeat step **FIVE** for flow around drill pipe in the open and cased hole sections.

- 7. Add the values from step 1 to 5, call these system losses.
- 8. Determine the pressure drop available for the bit = pump pressure system losses.
- 9. Determine nozzle velocity, total flow area and nozzle sizes.



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## BINGHAM PLASTIC MODEL

#### **A) Pipe Flow**

• Determine average velocity and critical velocity (Ý and V<sub>c</sub>):

•  $\acute{V} = \frac{24.5 \times Q}{D^2}$ ,

• 
$$V_{C} = \frac{97 PV + 97 \sqrt{PV^2 + 8.2 * \rho * D^2 * Y_{P}}}{\rho * D}$$

• If 
$$\acute{V} > V_c$$
, flow is turbulent; use  $P = \frac{8.91 \times 10^{-5} \rho^{0.8} Q^{1.8} P V^{0.2} L}{D^{4.8}}$   
• If  $\acute{V} < V_c$ , flow is laminar; use  $P = \frac{L*PV*V'}{90000D^2} + \frac{L*Y_p}{225*D}$ 



#### BINGHAM PLASTIC MODEL

**A)** Annular Flow

• Determine average velocity and critical velocity (Vand V<sub>c</sub>):

• 
$$\hat{\mathbf{V}} = \frac{24.5 \times Q}{Dh^2 - OD^2}$$
  $\mathbf{V}_{\mathbf{C}} = \frac{97 \, PV + 97 \sqrt{PV^2 + 6.2 * \rho * D_e^2 * Y_P}}{\rho * D_e}$ 

Where:  $\mathbf{D}_{\mathbf{e}} = \mathbf{D}_{\mathbf{h}} - \mathbf{O}\mathbf{D}$ 

• If 
$$\acute{V} > V_c$$
, flow is turbulent; use  $\mathbf{P} = \frac{8.91 \times 10^{-5} \rho^{0.8} Q^{1.8} P V^{0.2} L}{(D_h - O_D)^3 (D_h + O_D)^{1.8}}$ 

• If 
$$\acute{V} < V_c$$
, flow is laminar; use  $P = \frac{L*PV*V'}{60000 D_e^2} + \frac{L*Y_p}{225 D_e}$ 



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